

2 Functions

2.1 Introduction

1. Which of the following relations are functions?











2. State whether the following functions injective, surjective, bijective or neither.

2.2 Composition of Functions

1. $f: x \rightarrow : 2x - 1$ and $g: x \rightarrow 3 - 5x$ are two functions. Find i. f(4)ii. gf(4)iii. fg(-1)iv. gf(x). For what value of x is fg(x) = 25? 2. If $f(x) = x^2 - 1$ and g(x) = 3x + 2, find the value of each of the following: i. f(2)ii. gf(2)iii. g(4)iv. fg(4)v. $f^2(3)$ vi. $g^2(3)$

- vii. gf(-5)
- viii. $fg(\frac{2}{3})$
- 3. If f(x) = 4x 3, find
 - i. f^2x
 - ii. f^3x
 - iii. f^4x .

Hence, find an expression for $f^n(x)$ in terms of n.

2.3 Inverse Functions

1. Find the inverse of each of the following functions.

i.
$$f(x) = 2x$$

ii. $g(x) = x + 4$
iii. $h(x) = 2x - 1$
iv. $k(x) = 3x + 5$
v. $f(x) = 2 - 3x$
vi. $g(x) = \frac{4}{x}, x \neq 0$
vii. $h(x) = \frac{1}{x-2}, x \neq 2$
viii. $k(x) = \frac{x-5}{x}, x \neq 0$
ix. $g(x) = \frac{2x}{3x-2}, x \neq \frac{2}{3}$
x. $f(x) = 1 + \frac{1}{x}, x \neq 0$

- 2. Find the inverse function of each of the following by completing the square:
 - i. $f(x) = x^2 + 6x 10, x \ge -3$ ii. $f(x) = x^2 - 4x - 5, x \ge 2$ iii. $f(x) = x^2 - 10x + 13, x \ge 5$ iv. $f(x) = x^2 + 8x + 8, x \ge -4$
- 3. Given $f(x) = \frac{4-x}{3}, -1 \le x \le 4$. Sketch the graph of the given function and on the same set of axes, sketch the graph of the inverse function. State the domain and range of the inverse function.
- 4. Let $f : A \to R$, $f(x) = \sqrt{2-x}$. If A is the set of all real values of x for which f(x) is defined, find A.