

# Co-ordinate Geometry of the Circle

## 1 Centre (0,0) and radius $r$

- What is the equation of a circle with:
  - Centre (0,0) and radius = 5
  - Centre (0,0) and radius = 4
  - Centre (0,0) and radius = 10
  - Centre (0,0) and radius = 2
  - Centre (0,0) and radius =  $\sqrt{10}$
  - Centre (0,0) and radius =  $\sqrt{2}$
  - Centre (0,0) and radius =  $\sqrt{5}$
- What is the centre and radius of the following circles?
  - $x^2 + y^2 = 25$
  - $x^2 + y^2 = 81$
  - $x^2 + y^2 = 169$
  - $x^2 + y^2 = 2$
  - $x^2 + y^2 = 20$
  - $x^2 + y^2 = 1$
- Find the four co-ordinates, where each of the following circles cut the  $x$ -axis and the  $y$ -axis. Hence draw a rough sketch of each circle.
  - $x^2 + y^2 = 25$
  - $x^2 + y^2 = 81$
  - $x^2 + y^2 = 169$
- Find the equation of a circle with:
  - Centre (2,3) and radius = 5
  - Centre (1,4) and radius = 4
  - Centre (-2,-1) and radius = 10
  - Centre (-3,3) and radius = 12
  - Centre (5,-6) and radius =  $\sqrt{10}$
  - Centre (0,-3) and radius =  $\sqrt{2}$

(g) Centre (2,0) and radius =  $\sqrt{50}$

5. What is the centre and radius of the following circles?

(a)  $(x - 2)^2 + (y - 3)^2 = 100$

(b)  $(x - 4)^2 + (y - 1)^2 = 64$

(c)  $(x + 3)^2 + (y + 2)^2 = 25$

(d)  $(x + 1)^2 + (y + 7)^2 = 10$

(e)  $(x - 5)^2 + (y + 4)^2 = 81$

(f)  $(x + 2)^2 + (y - 2)^2 = 49$

(g)  $x^2 + y^2 = 25$

(h)  $x^2 + (y - 3)^2 = 16$

(i)  $(x + 1)^2 + y^2 = 20$

6. Find the equation of the circle with:

(a) Centre (0, 0) and containing the point (3,4)

(b) Centre (0, 0) and containing the point (-5,12)

(c) Centre (3, 2) and containing the point (-1,5)

(d) Centre (-7, -2) and containing the point (-1,6)

(e) Centre (0, -5) and containing the point (2,-1)

7. Find the coordinates of the points of intersection of the line and the circle:

(a) Line:  $x + y - 7 = 0$ , Circle:  $x^2 + y^2 = 5$

(b) Line:  $x + y - 5 = 0$ , Circle:  $x^2 + y^2 = 13$

(c) Line:  $x + y + 3 = 0$ , Circle:  $x^2 + y^2 = 65$

(d) Line:  $x - y - 2 = 0$ , Circle:  $x^2 + y^2 = 2$

(e) Line:  $x - 3y = 10$ , Circle:  $x^2 + y^2 = 10$